



2. (16 pts) OpenMP loop optimizations. Read both subparts first before answering question.

```
for (j=0; j<n; j++) {  
  for (i=0; i<m; i++) {  
    sum = sum + a[j*m+i]  
  }  
}
```

(a) Rewrite this code snippet to parallelize the loop using OpenMP and use an OpenMP reduction to eliminate the separable dependency among loops.

(b) Coalesce the loop to optimize your rewritten code. Hint: This conversion will allow OpenMP to realize balanced parallelism even when  $n$  is smaller than the number of cores in your machine.

3. (16 pts) On loop efficiency in the cache hierarchy

- (a) Why are the nested loops of the previous problem more efficient than the following loop that switches the iteration order.

```
for (i=0; i<m; i++) {  
  for (j=0; j<n; J++) {  
    sum = sum + a[j*m+i]  
  }  
}
```

- (b) Estimate the relative performance of the nested loop in the previous problem and the nested loop in this problem. Assume that a  $i$  and  $j$  are 64-bit integers and that L1 cache line contains 128 bytes. You should also assume that the L3 cache is too small to hold  $n$  or  $m$  items. Show your work.



5. 16 pts Draw a speedup chart for a parallel algorithm with an Amdahl number  $p = 0.8$ . Label the value of two specific points in your chart—typically  $(1,1)$  and  $(x,y)$  that solves Amdahl's equation. What is the asymptotic speedup of this algorithm as available resources become infinite? Include dashed reference lines in your chart for ideal speedup and asymptotic performance.

Scratch space.